#### Year 2

## **Multiplication as Repeated Addition**



Group Equal Unequal Repeated Addition Multiplication Expression Equation Part Altogether Represents Amount Size



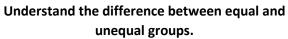












The \_\_\_ have been grouped.



We can represent equal groups as repeated addition.

There are 3 groups of 5.

$$5 + 5 + 5$$

$$3 \times 5$$

$$5 + 5 + 5 = 3 \times 5$$

We can represent repeated addition using

a multiplication expression.

The 3 represents the number of groups.

The 5 represents the number of eggs in each group.

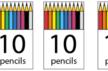
each group.

represents the total number of \_\_\_\_.

The \_\_\_\_ represents the number of groups.

The \_\_\_ represents the number of \_\_\_\_ in

















9 × 10

We can skip count in multiples of \_\_\_ to work out the total amount.

10, 20, 30, 40 ... there are 90 pencils altogether.















15 represents the total number of eggs.

Notice how the representations allow the children to see each of the numbers (i.e. 10 pencils and 9 packets).

#### Year 2

Grouping problems: missing factors and division

#### Vocabulary:

Multiplication Division Factor 'divided by' Represents Skip Counting

Multiplication facts Groups Amount Size

# 





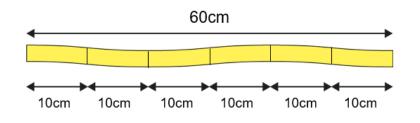


We can solve division problems by finding missing factors.

The 15 represents the number of biscuits.

The 5 represents the number of biscuits in each bag (group).

The 3 represents the number of bag (groups).



6 × 10 = 60

We can use  $\div$  to mean 'divided by'

We can use our knowledge of times tables to help solve division problems.

The 60cm represents the length of the ribbon.

The 10 represents the size of each piece.

The 6 represents the number of pieces we can make.

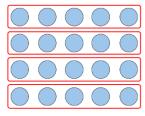
#### Year 3

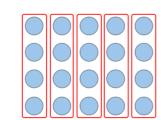
# **Multiplication and Division Structures**

#### Vocabulary:

Multiplication Division Commutative Grouping (Quotitive) Sharing (Partitive)

'Divided into'	'Divide	d between'	'Divided by'		Equation	Factor	Product
		30	÷	5	=	6	
		dividend	÷	divisor	=	quotient	



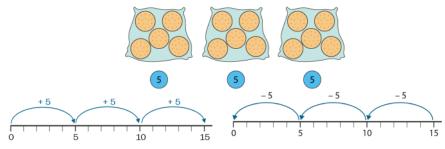


Identify that multiplication is commutative.

 $4 \times 5 = 5 \times 4$ 

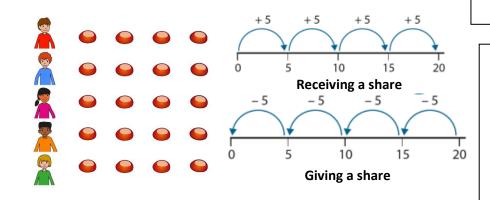
Factor times factor is equal to product.

The order of the factors does not affect the product.



Making groups of

Removing groups of



Division equations can be used to represent 'grouping' problems.

We can use multiplication facts to find the number of groups.

(Quotitive division)

15 divided into groups of 5 is equal to 3.

$$5+5+5=15$$
  
 $15-5-5-5=0$   
 $15 \div 5=3$ 

Division equations can be used to represent 'sharing' problems.

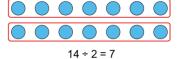
We can use multiplication facts to find the size of groups.

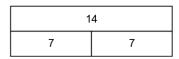
(Partitive division)

Four fives are four each.

20 divided between 5 is equal
to 4 each.

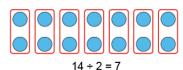
20 ÷ 5 = 4





The same equation can be represented in both grouping and sharing contexts.

7 times 2 is 14, so  $14 \div 2 = 7$ 



		14			
2	2	2	2	2	2

#### Year 4

# Multiplying and Dividing by 10 and 100

#### Vocabulary:

Multiply Divide Unitise Ten/Hundred times Bigger Smaller One-tenth the size One-hundredth the size Gattegno chart Factor Product Multiple Groups of Inverse

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

#### Develop language in order to multiply and divide by 10 or 100.

80 is ten times bigger than 8. 8 is ten times smaller than 80. 80 is ten times the size of 8 8 is one-tenth the size of 80.

800 is one hundred times bigger than 8. 8 is one hundred times smaller than 800. 800 is on hundred times the size of 8 8 is one-hundredth the size of 80.

> $8 \times 1 = 8$ 8 x 1 ten - 8 tens 8 x 1 hundred = 8 hundreds

#### Generalisations

All multiples of 10 have a ones digit of zero.

All multiples of 100 have both a tens and ones digit of zero.

To find the inverse of \_\_\_times as many, you divide by \_\_\_\_.

If one factor if made \_\_\_\_ times bigger/smaller then the product will be ten times bigger/smaller



ten times the size

x10

÷10

one-tenth of the size

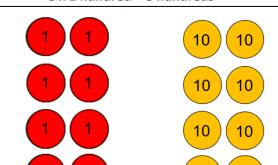
1,000s	100s	10s	1s
			8
		8	0
			1

1,000s	100s	10s	1s
			8
	8	0	0
	8	U	U

÷100

one-hundredth of the size

one hundred times the size x100



$$8 \times 1 = 8 \quad 8 \times 10 = 80 \quad 8 \times 100 = 800$$

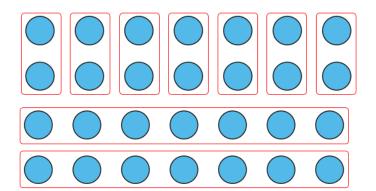
8 groups of is .

Year 4

**Manipulating the Multiplicative Relationship** 

#### Vocabulary:

Multiply Divide Commutative Groups of Equal to Times Factors Product Quotient Dividend Divisor Represents Array



$$2 \times 7 = 7 \times 2$$

Understand that multiplication is commutative and the factors can be

2 groups of 7 is equal to 14.

2, 7 times is equal to 14.

2 groups of 7 is equal to 7, two times.





$$2 \times 7 = 14$$

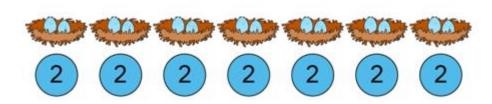


$$7 \times 2 = 14$$

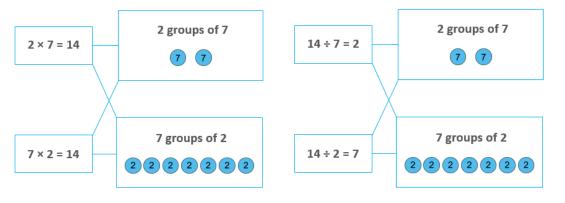
The 2 represents \_\_\_\_.

The 7 represents \_\_\_\_.

The 14 represents \_\_\_\_.



### Match equations to representations and contexts.

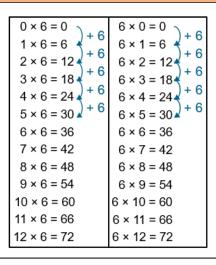


Year 4

# The Distributive Property of Multiplication

#### Vocabulary:

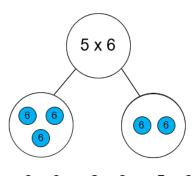
Multiplication Distributive Law Adjacent Multiples Factors Partitioning **Equations** Expressions Arrays Part-whole model Difference



×	1	2	3	4	5	6
1		•	•	•		•
2						
3	•	•		•	•	
4						
5	•	•		•		•

 $4 \times 6 + 6$ 

Five sixes is one more six than four sixes.



 $3 \times 6 + 2 \times 6 = 5 \times 6$ 

5 is equal to 3 plus 2, so 5 sixes is equal to 3 sixes plus 2 sixes.

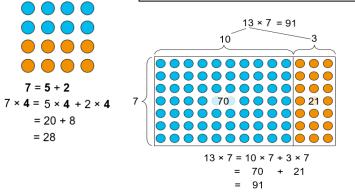
Adjacent multiples of \_\_\_ have a difference of \_\_\_.

7 = 5 + 2

= 20 + 8

= 28

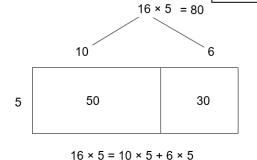
We can partition one of the factors to make calculations easier.





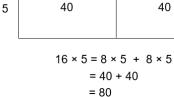
$$9 = 10 - 1$$
 $9 \times 4 = 10 \times 4 - 1 \times 4$ 
 $= 40 - 4$ 
 $= 36$ 

We can partition the factors in different ways to make calculations easier.



= 50 + 30

= 80



 $16 \times 5 = 80$ 

Year 5

Multiplying and Dividing by 10 and 100 (1)

#### Vocabulary:

Multiply Divide Unitise Ten/Hundred times Bigger Smaller One-tenth the size One-hundredth the size Gattegno chart Factor Product Multiple Groups of Inverse Ones Tens Hundreds Tenths Hundredths

 $8 \div 10 =$  $0.8 \div 10 =$ 

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000		
100	200	300	400	500	600	700	800	900		
10	20	30	40	50	60	70	80	90		
1	2	3	4	5	6	7	8	9	١	
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	)	÷ 10
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09		÷ 10 one-tenth
										the size

 $0.08 \times 10 =$  $0.8 \times 10 =$ 

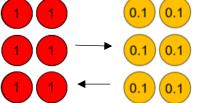
1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000	
100	200	300	400	500	600	700	800	900	
10	20	30	40	50	60	70	80	90	
1	2	3	4	5	6	7	8	9	7
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09	

× 10 ten times the size

× 10

 $8 \div 10 = 0.8$ 

one-tenth of the size



 $0.8 \times 10 = 8$ 

ten times the size

We can multiply and divide a number by 10.

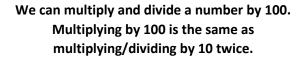
8. made one-tenth the size is 0.8.

8 divided by 10 is 0.8.

First we had 8 ones, now we have 8 tenths.

 $8 \div 100 = 0.08$ 

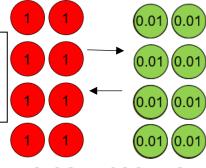
one-hundredth of the size



8, made 100 times smaller is 0.08.

8 divided by 100 is 0.08.

First we had 8 ones, now we have 8 hundredths



 $0.08 \times 100 = 8$ 

one hundred times the size

Year 5

# Multiplying and Dividing by 10 and 100 (2)

#### Vocabulary:

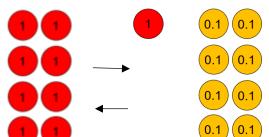
Multiply Divide Unitise Ten/Hundred times Bigger Smaller One-tenth the size One-hundredth the size Gattegno chart Factor Product Multiple Groups of Inverse Ones Tens Hundreds Tenths Hundredths

$$3.6 \times 10 = 36$$
  
 $36 \div 10 = 3.6$ 

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

1.8 is one-tenth the size of 18 18 divided by 10 is 1.8.



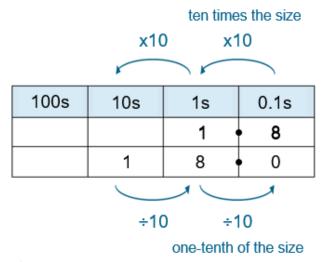


\_\_ divided by 10/100 is equal to\_\_.

\_\_ is one-tenth/hundredth the size of \_\_.

\_\_ multiplied by 10/100 is equal to\_\_.

\_\_ is 10/100 times the size of \_\_.



 $1.8 \times 10 = 18$ 

ten times the size

We can multiply and divide numbers with digits greater than 0 by 10 or 100.

#### Generalisation

To multiply by 10, move each digit one place to the left.

To multiply by 100, move each digit two places to the left.

To divide by 10, move each digit one place to the right.

Year 5

Multiplying and Dividing by 10 and 100 (3).

#### Vocabulary:

Multiply Divide Unitise Ten/Hundred times Bigger Smaller One-tenth the size One-hundredth the size Gattegno chart Factor Product Multiple Groups of Inverse Ones Tens Hundreds Tenths Hundredths

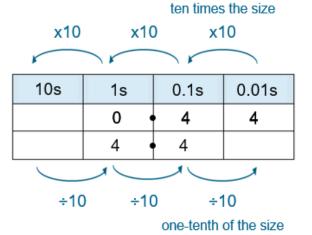
$$0.27 \times 10 = 2.7$$

$$2.7 \div 10 = 0.27$$

1,000	2,000	3,000	4,000	5,000	6,000	7,000	8,000	9,000
100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9
0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09

0.27 is one-tenth the size of 2.7

2.7 divided by 10 is 0.27.



$$4.4 \div 10 = 0.44$$

one-tenth of the size

- 1
- 0.1
- 0.1
- 0.01

- 1
- 0.1
- 0.01

- 0.1
- 0.01
- 0.1
- 0.01

$$0.44 \times 10 = 4.4$$

ten times the size

We can multiply and divide numbers with digits greater than 0 by 10 or 100.

divided by 10/100 is equal to\_\_.

\_\_ multiplied by 10/100 is equal to\_\_.

 $\underline{\phantom{a}}$  is 10/100 times the size of  $\underline{\phantom{a}}$ .

\_\_ is one-tenth/hundredth the size of \_\_.

#### Generalisation

To multiply by 10, move each digit one place to the left.

To multiply by 100, move each digit two places to the left.

To divide by 10, move each digit one place to the right.

Year 5

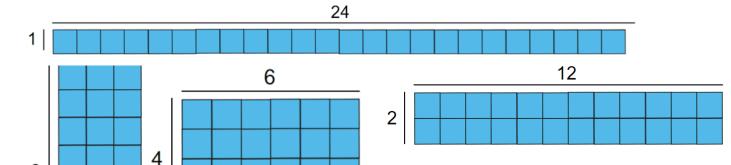
**Find Factors and Multiples** 

#### Vocabulary:

Factor Multiple Composite Square Prime Common Factor Prime Factor
Factor Bug Array Positive Integer Working Systematically

Factor x Factor = Product

Dividend ÷ Divisor = Quotient



 $8 \times 3 = 24$ 

 $4 \times 6 = 24$ 

 $2 \times 12 = 24$ 

 $1 \times 24 = 24$ 

There are \_\_\_\_ tiles. There are \_\_\_\_ rows and \_\_\_\_ columns. So \_\_\_\_ and \_\_\_ are factors of \_\_\_\_.

Generalise: Numbers that have more than two factors are composite numbers.

Manipulate the array and write the equations to support each representation.

Factor x Factor = Product

Use factor bugs to record pairs of factors.



8

$$1 \times 1 = 1$$

#### **Generalise:**

When one is a factor, the product is equal to the other factor.

All positive integers have a factor of 1.

Every positive integer is a factor of itself.

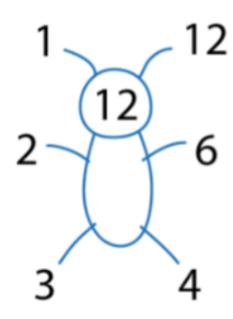
The smallest factor of a positive integer is always 1.

The largest factor of a positive integer is always itself.









Year 5

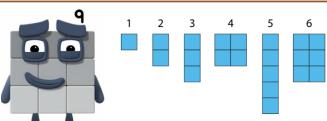
# **Find Factors and Multiples**

#### Vocabulary:

Factor Multiple Composite Square Prime Common Factor Prime Factor
Factor Bug Array Positive Integer Working Systematically

Factor x Factor = Product Dividend ÷ Divisor = Quotient





Extend this to square numbers, and prime numbers recognising the number of factors.

	×	0	1	2	3	4	5	6	7	8	9	10	11	12
	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	1	0	1	2	3	4	5	6	7	8	9	10	11	12
	2	0	2	4	6	8	10	12	14	16	18	20	22	24
	3	0	3	6	9	12	15	18	21	24	27	30	33	36
	4	0	4	8	12	16	20	24	28	32	36	40	44	48
	5	0	5	10	15	20	25	30	35	40	45	50	55	60
	6	0	6	12	18	24	30	36	42	48	54	60	66	72
	7	0	7	14	21	28	35	42	49	56	63	70	77	84
ĺ	8	0	8	16	24	32	40	48	56	64	72	80	88	96
ĺ	9	0	9	18	27	36	45	54	63	72	81	90	99	108
	10	0	10	20	30	40	50	60	70	80	90	100	110	120
ĺ	11	0	11	22	33	44	55	66	77	88	99	110	121	132
-	12	0	12	24	36	48	60	72	84	96	108	120	132	144
•			$\overline{}$											

Make connections with factors and times tables. Make connections with factors of factors

\_\_\_ is a factor of \_\_\_ because it is in the \_\_\_ times table.

Nine is a factor of all of these numbers.

Three is a factor of nine which means it is also a factor of all of these numbers.

Is 9 a factor of 54?

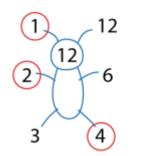
54 ÷ 9 = 6

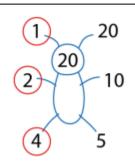
9 and 6 are factors of

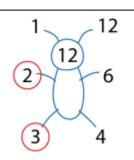
54.

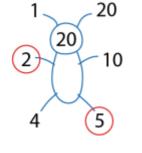
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Use factor bugs to find common factors and prime factors.









#### Year 5

# **Find Factors and Multiples**

#### Vocabulary:

Factor Multiple Composite Square Prime Common Factor Prime Factor
Factor Bug Array Positive Integer Working Systematically

Factor x Factor = Product

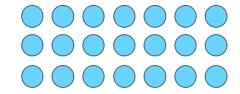
Dividend ÷ Divisor = Quotient



3

#### **Introduce Multiples**

is a factor of because x =
is a multiple of because x =
is a factor of because ÷ =
is a multiple of because ÷ =



#### $7 \times 3 = 21$

Make statements about factors and multiples whilst increasing the amount of each counter in the array.

- \_\_\_\_ represents the number of counters in each row.
- \_\_\_ represents the total value of the counters in each column.
  - \_\_\_\_ represents the total value of the counters.

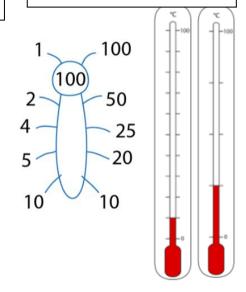
3, 7, 10, 21 and 70 are factors of 210.

210 is a multiple of 3, 7, 10, 21 and 70.

# Identify Common Multiples using a 100 square.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

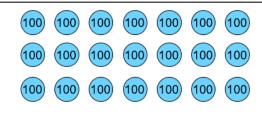
# Factors of 100 can be applied to contexts



$$7 \times 30 = 210$$

$$70 \times 3 = 210$$

$$10 \times 21 = 210$$



$$7 \times 300 = 2{,}100$$

$$700 \times 3 = 2,100$$

$$100 \times 21 = 2{,}100$$

#### **Multiplication and Division** Vocabulary: Ones Tens Hundreds Thousands Represents Partition Recombine Year 5 Multiply Unitising Partial Product Aligned Calculation Expanded layout Compact layout Equation Regroup Algorithm Multiply using a Formal Written Method (1) Factor x Factor = Product 34 chairs 10s 1s 3 2 rows 4 Move between representations of dienes and expanded written multiplication. Use dienes to represent context as 10s repeated addition and move to multiplication. 34 = 30 + 4 $34 \times 2 = 30 \times 2 + 4 \times 2$ $2 \times 4$ ones = 8 ones $2 \times 4$ ones = 8 ones 963 $321 \times 3 =$ 10s 1s 6 $7 \times 3$ tens = 6 tens 100s 10s 1s 3 2 $3 \times 1$ ones = 3 ones X $0.3 \times 2 \text{ tens} = 6 \text{ tens}$ 0 3 × 3 hundreds = 9 hundreds 6 9 6 3 Represent 3 digit by 1 digit $2 \times 4$ ones = 8 ones Move between representations of 3 2 1 multiplication without exchanges using expanded layout and compact $2 \times 3$ tens = 6 tens dienes, moving from expanded layout layout. 6 8 6 3 to compact layout.

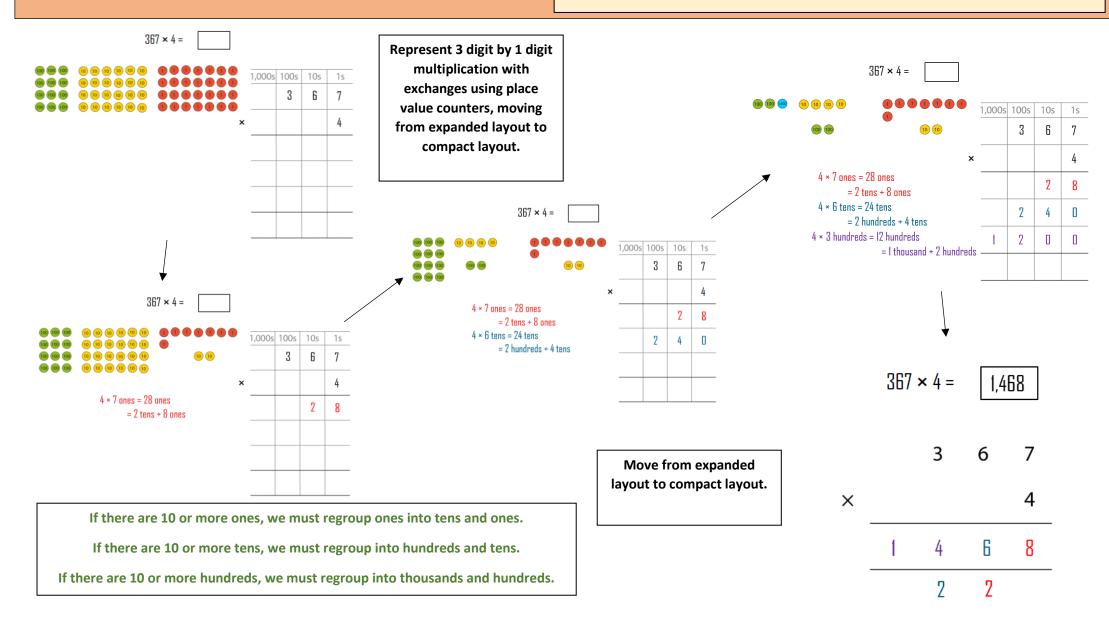
#### Year 5

## Multiply using a Formal Written Method (2)

#### Vocabulary:

Ones Tens Hundreds Thousands Represents Partition Recombine Multiply Unitising Partial Product Aligned Calculation Expanded layout Compact layout Equation Regroup Algorithm

Factor x Factor = Product



#### Year 5

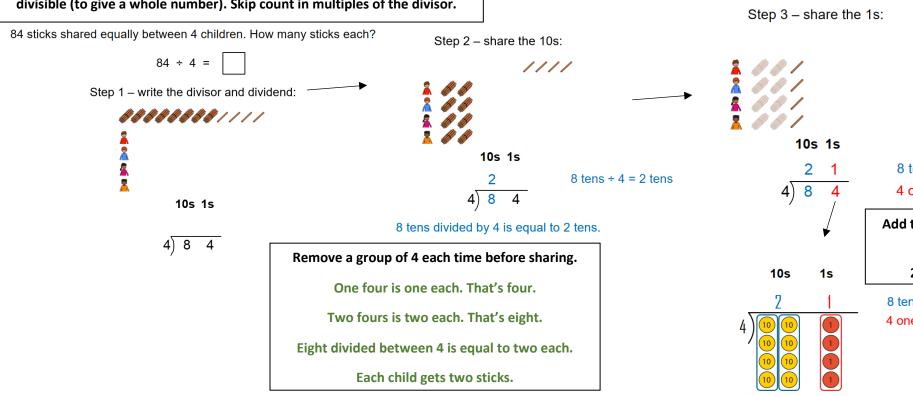
# **Divide using a Formal Written Method (1)**

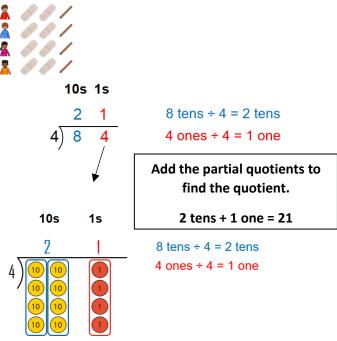
#### Vocabulary:

Partitive (sharing) Quotitive (grouping) Ones Tens Hundreds Thousands Represents Divide Unitising Dividend Divisor Quotient Partial Quotient Aligned Calculation Equation Exchange Algorithm 'Sharees' Divisible Remainder 2 1 4) 8 4 **Short Division** 

auotient divisor)dividend

Use sticks to represent partitive (sharing) context where the dividend is divisible (to give a whole number). Skip count in multiples of the divisor.





#### Year 5

# **Divide using a Formal Written Method (2)**

#### Vocabulary:

Partitive (sharing) Quotitive (grouping) Ones Tens Hundreds Thousands
Represents Divide Unitising Dividend Divisor Quotient Partial Quotient
Aligned Calculation Equation Exchange Algorithm 'Sharees' Divisible Remainder
Short Division

72 sticks shared equally between 3 children. How many sticks each?

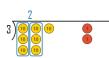
Step 1 – write the divisor and the dividend:



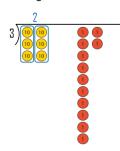


Step 2 - share the 10s:





2 3) 7 <sup>1</sup>2



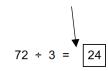
 $7 \text{ tens} \div 3 = 2 \text{ tens } r \text{ 1 ten}$ 

Use sticks and place value counters to represent partitive (sharing) context where the dividend is divisible (to give a whole number) though requires an exchange from the tens. Skip count in multiples of the divisor.

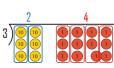
If dividing the tens gives a remainder of one or more ten, we must exchange the remaining tens for ones.

 $7 \text{ tens} \div 3 = 2 \text{ tens } r \text{ 1 ten}$ 

Step 3 – exchange:

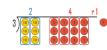


Step 4 – share the 1s:



73 ÷ 3 = 24 r 1

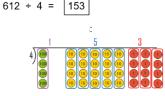




7 tens  $\div$  3 = 2 tens r 1 ten 13 ones  $\div$  3 = 4 ones r 1 one Apply the same representations though this time include a remainder.

Then extend to division of 3 digits by one digit and where there can be no hundreds cannot be shared.

If dividing the hundreds gives a remainder of one or more hundred, we must exchange the remaining hundreds for tens.



6 hundreds ÷ 4 = 1 hundred r 2 hundreds 2 hundreds = 20 tens 21 tens ÷ 4 = 5 tens r 1 ten 1 ten = 10 ones 12 ones ÷ 4 = 3 ones 7 tens  $\div$  3 = 2 tens r 1 ten 12 ones  $\div$  3 = 4 ones

### Addition, Subtraction, Multiplication and Division

#### Year 6

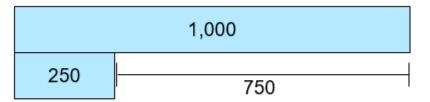
# Quantify additive and multiplicative relationships

#### Vocabulary:

Additive Multiplicative Relationship Represents Compose Combine Total More than Less than Plus + Minus - Equal to = Addition Subtraction Divide ÷ Multiply x One-\_\_\_\_ of Equation Expression Bar Model Whole Part Difference Multiplier Unknown Sequence

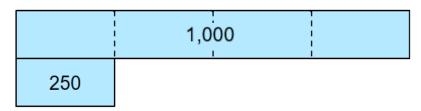
Addend + Addend = Sum Factor x Factor = Product (Multiplicand x Multiplier = Product)

Minuend – Subtrahend = Difference Dividend ÷ Divisor = Quotient



$$250 + 750 = 1,000$$

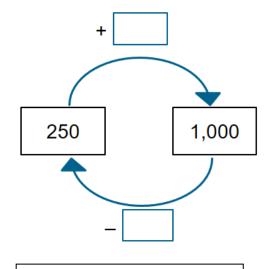
$$1,000 - 750 = 250$$



$$250 \times 4 = 1,000$$

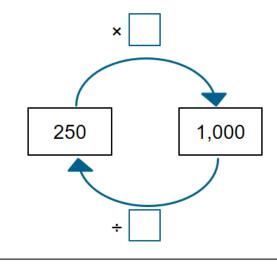
$$1000 \div 4 = 250$$

The relationship between two numbers can be expressed both additively and multiplicatively.



1000 is \_\_\_ more than 250.

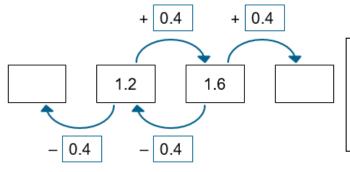
250 is \_\_\_\_ less than 1000.



1000 is \_\_\_\_ times the size of 250.

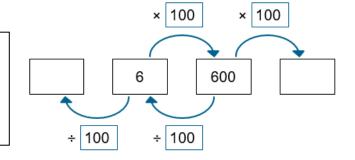
250 is one-\_\_\_\_ of 1000.

To find one-quarter of a number, we divide by 4.



Finding the difference can help calculate the unknown terms in a sequence.

Finding the known multiplier can help calculate the unknown terms in a sequence.



# Addition, Subtraction, Multiplication and Division

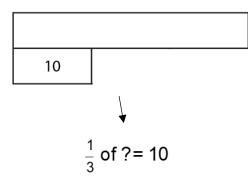
### Year 6

## Quantify additive and multiplicative relationships

Calculate the unknown whole by recognising

how many parts the whole has been divided into.





30								
10	10	10						

$$\frac{1}{3}$$
 of  $30 = 10$ 

#### Vocabulary:

Additive Multiplicative Relationship Represents Compose Combine Total More than Less than Plus + Minus - Equal to = Addition Subtraction Divide ÷ Multiply x One-\_\_\_\_ of Equation Expression Bar Model Whole Part Difference Multiplier Unknown Sequence

Addend + Addend = Sum Factor x Factor = Product (Multiplicand x Multiplier = Product)

Minuend – Subtrahend = Difference Dividend ÷ Divisor = Quotient

### **Addition and Subtraction**

### Year 6

### **Derive Related Calculations**

#### Vocabulary:

Additive Multiplicative Relationship Represents Equation Unknown Rearrange Inverse Place Value Properties Commutative Associative Distributive Compensation

Addend + Addend = Sum Factor x Factor = Product (Multiplicand x Multiplier = Product)

Minuend – Subtrahend = Difference Dividend ÷ Divisor = Quotient

$$252 = 3 \times 84$$

$$252 = 3 \times 84$$

$$252 = 3 \times 84$$

$$625 - 148 = 477$$

$$625 - 148 = 477$$

$$625 - 148 = 477$$

Multiplicative examples

Manipulate an equation to solve another. Pupils could:

rewrite using inverse operations;

to the commutative, associative or distributive property of multiplication; use the compensation property.

use the properties of division that correspond

rearrange the terms;

apply place value;

$$14.8 + 7.6 = 22.4$$

$$14.8 + 7.6 = 22.4$$

$$4,800 \div 25 = 192$$

$$4,800 \div 25 = 192$$

$$4,800 \div 25 = 192$$

### **Addition and Subtraction**

### Year 6

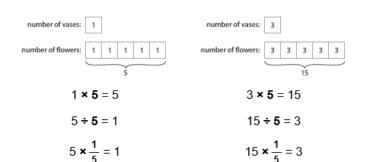
# **Solve Problems involving Ratio Relationship**

#### **Vocabulary:**

Additive Multiplicative Relationship Represents Equation Unknown Scalefactor Ratio Ratio Table \_\_\_\_ times the size one-\_\_\_ the size of Vertical Horizontal

Factor x Factor = Product (Multiplicand x Multiplier = Product)

Dividend ÷ Divisor = Quotient



Ratio table to compare sets of information.

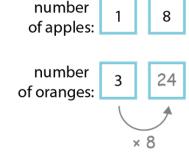
For every \_\_\_\_, there are \_\_\_\_.

For every 1 litre of petrol, you can drive 7 miles.

For every 7 miles you will drive, you need 1 litre of petrol.

Extend sequences using knowledge of patterns based on ratio table.

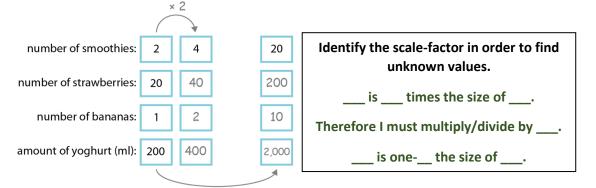
Litres of petrol	1	2	3	4	5	6	7	8	9	10
Miles driven	7	14	21	28	35	42	49	56	63	70



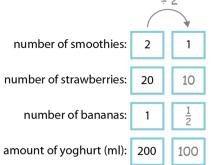
number of apples:	1	8	
number of oranges:	3	24	× 3

Explore vertical and horizontal relationship between numbers.

For every \_\_\_\_, there are \_\_\_\_.



× 10



### **Addition and Subtraction**

### Year 6

### **Solve Problems with Two Unknowns**

#### Vocabulary:

Additive Multiplicative Relationship Represents Equation Two Unknowns Scale-factor Ratio \_\_\_\_ times the size one-\_\_\_ the size of Total Bar Model Structure



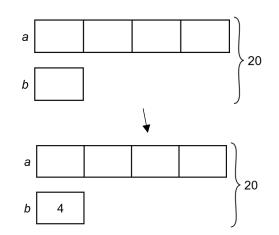
$$B = r + b$$

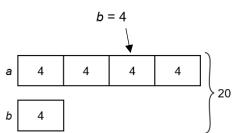


There is more than one solution to the problem.

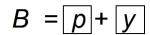
There can be infinite solutions to a problem.

# Solve multiplicative problems with two unknowns when the total is known.

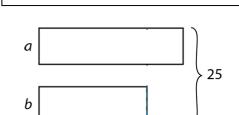


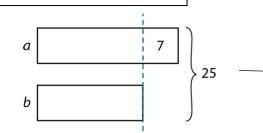


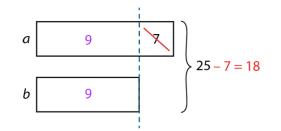
one part = 
$$20 \div 5 = 4$$
  
  $b = 4$ 



Solve additive problems with two unknowns when the total is known.







$$b = 18 \div 2 = 9$$

$$a = 9 + 7 = 16$$

The two numbers are 9 and 16.